

Grade 3 | Module 2

Topic: Partitioning a whole into equal sections (fractions)

Students use their understanding of fair sharing whole numbers into equal groups to partition one whole into equal fractional sections. Students partition a whole into halves, thirds, fourths, and eighths. They understand that a fraction 1/b is the quantity formed by 1 part of a whole partitioned into b equal parts. Students work with puzzles that involve selecting a fraction of size 1/b to create a fraction a/b (b>0).

Module 2 at a Glance

Printed Resources

Bookmarks

- Problem Solving Process Bookmark
- Problem Solving Facilitation Bookmark

• Grades 3–5 Table Games

- Equivalent Fraction Concentration
- Multiplication Connect Four
- Traffic Lights Tic-Tac-Toe (optional)
- Dara (optional)
- Number Line Fraction Bingo (Day 5)
- Final Countdown (Day 5)

- Problem Solving Journal (pages 8–13)
 - My Thinking Path
 - Problem of the Day
 - Exit Tickets
 - ST Math Reflections
- Design Challenge Station Booklet
 - Pages 8–14

Optional Printed Resources

- Accomplishments Log
- ST Math Activity Pages
- Pre/Post Quizzes

Teacher Resources

• Teacher Planner

Immersion Slide Deck (slides 15–27)

• The Immersion Slide Deck is intended to be projected to the class in a whole group setting.

Supplies

• Paper fraction strips or other fraction model manipulatives

Supplies for Table Games (per group)

- Equivalent Fraction Concentration 1 deck of Equivalent Fractions cards (2 sheets cut)
- Multiplication Connect Four 2 paper clips, 2 sets of 20 colored game pieces or chips (different colors), 1 printed Multiplication Connect Four Game Board.

My Thinking Path

• This module, students reflect on partitioning a whole into equal sections (fractions).

ST Math Puzzle Talks

- Pie Monster
- Match Fractions



Modul

Problem Solving

Day 1:

• **Problem of the Day** - Joe the baker baked 2 apple pies for the Hughes family. There are 8 people in the Hughes family. The family shared the pies equally. How much pie did each family member get?

Day 2:

• **Problem of the Day** - Joe the baker baked 7 apple pies to sell in his shop. Four people came in at the same time to buy pie. Joe sold the 7 pies to the four people. Each person got an equal amount of pie. How much pie did each person buy?

Day 3:

• **Problem of the Day** - Gordon baked a pan of lasagna for his family of 4. He cut the lasagna into eight equal pieces. Explain how much lasagna each family member might eat.

Day 4:

• **Problem of the Day** - Brett and 3 classmates were given a bulletin board to present their Math Challenge. They decided to divide the bulletin board so that each of them had an equal amount of space. Show two different ways they could partition the board. Prove that one partition from your first bulletin board example is equivalent to one partition from the second example.

Instructional Stations

On Days 1–4, each student will visit two stations a day for 20 minutes each. On Day 5, students do not rotate. They can either be assigned to a station or allowed to choose one to go to. Consider assigning students who need additional support to Station 1 to work with the teacher on concepts they are struggling with.

 Station 1: Small Group Instruction Days 1 & 2: Show and work through puzzles from Balance Pies Days 3 & 4: Show and work through rich problems similar to the Problems of the Day. 	 Station 2: ST Math Puzzles Have students sign in and play ST Math puzzles. Remind students to use manipulatives and/or paper and pencil to help them solve problems. With 5 minutes left, have students stop playing and complete their Puzzle Reflection and Accomplishments Log.
 Station 3: Table Games Select Equivalent Fraction Concentration or Multiplication Connect Four. Have students play that game. Ask students to complete an Exit Ticket during the final 5 minutes. 	 Station 4: Design Challenge Days 1 & 2: Have students think about how they might change a game. Days 3 & 4: Complete the Game Planning Mock Up sheet on page 8 in the Game Design Challenge Station booklet.

Day 5: Design Challenge Station (Whole Group)

- Discuss the importance of rules.
- Have the students work in groups to complete the Game Rules Challenge on page 9 of their Design Challenge Station Booklet.
- As students continue to work on their blueprints they need to ensure that they are making the clear rules and directions.





My Thinking Path (5-10 minutes)

- Remind students of the My Thinking Path page in their journal. Have them write in the topic, "Solving problems involving partitioning a whole into equal sections (fractions)."
- Have students work on the My Thinking Path page in their journals.
- Discuss their ideas, and allow students to add to their paper any additional thoughts they have.
- Begin each of Days 1–4 with time for students to reflect on their learning and prepare for the day.
- Have students complete the Pre-Quiz (optional).

Puzzle Talk: Pie Monster (20-25 minutes)

¤ Focus on student thinking and developing problem solving skills using the Problem Solving Process.

¤ Provide students with whiteboards/dry-erase markers.

Notice and Wonder

- Display the first puzzle in Level 1. Ask: "What do you notice? What do you wonder?" Allow a few students to share out.
- Ask students to think of their strategy for solving the puzzle and predict what will happen when they try it.

Predict and Justify

- Have students think-pair-share their strategy with a partner, explaining their reasoning.
- Have students share out. Ask the students to think about if they agree/disagree with the strategy and why. How does it relate to their strategy?

Test and Observe

- Try one of the students' ideas. (As you try students' strategies, be sure to try strategies that work and those that don't.)
- Watch the feedback together for correct and incorrect tries, and discuss what you saw.

Analyze and Learn

- Ask students to think about how what they saw happen compares to their prediction.
- Show another puzzle. Have students prepare to show how they would solve it.
- Share several examples. Look for students who also wrote the number, or ask students to write the number.
- Look for mixed numbers and a/b (b>0) fractions. Discuss counting fractions compared to counting whole numbers and equivalence. Ask how they know this fraction is equivalent to this mixed number (e.g., why is 2 the same as 4/2).

Connect and Extend

- Open up some puzzles from Level 2. (Make sure you include puzzles with thirds and fourths.) Have students do a think-pair-share with a partner about what they notice. How is it different from Level 1?
- Continue to show a few other puzzles in Level 2 (especially partitioned into halves).
 - $\circ\;$ Have students share ideas on how they would solve the puzzle.
 - Share out several examples. Look for students who also wrote the number, or ask students to write the number.
 - Look for mixed numbers and a/b fractions. Discuss counting fractions compared to whole numbers.
 Discuss the equivalence.
- Do the same as above, but with Puzzles from Level 3 showing thirds and fourths. Questions to ask: "How many thirds/halves/fourths did you need for each whole pie? How many thirds/halves/fourths are there altogether?"

How does the student:

- figure out how many unit fractions are needed for one whole?
- count unit fractions to find the total?
- understand that the a/b (b>0) fraction is equivalent to the mixed number?

Problem Solving (20-25 minutes)

Engage students in problem solving discussions. Read and discuss the problem, share student work, compare strategies, and make connections.

Problem of the Day

Joe the baker baked 2 apple pies for the Hughes family. There are 8 people in the Hughes family. The family shared the pies equally. How much pie did each family member get?

Instructional Stations (40 minutes)

Students will visit two stations today (20 minutes in each station). They will visit the other two tomorrow.

 Station 1: Small Group Instruction Work with students on the ST Math game, <i>Balance Pies</i>. Use the Problem Solving Process to discuss the game with the group. Work through Levels 2 on. Have students name fractions of pies. Discuss unit fractions and a/b (b>0) fractions. Students explore and discover how a/b (b>0) fractions are made up of a fractions of size 1/b. 	 Station 2: ST Math Puzzles Have students sign in and play ST Math puzzles. Remind students to use manipulatives and/or paper and pencil to help them solve problems. With 5 minutes left, have students stop playing and complete their Puzzle Reflection and Accomplishments Log.
 Station 3: Table Games Select Equivalent Fraction Concentration or Multiplication Connect Four. Have students play that game. Ask students to complete an Exit Ticket during the final 5 minutes. 	 Station 4: Design Challenge Have students select one of the games they played in the last module and replay it. After playing the game, have students discuss how they would change the game. Students make the changes and then try playing the game with their changes. Have them discuss how the changes affected gameplay. Did they like them? Did they not like them? Did it make it easier or harder?





My Thinking Path (5-10 minutes)

• Have students reflect on what they have learned about solving problems involving partitioning a whole into equal sections (fractions).

Puzzle Talk: Pie Monster (20-25 minutes)

process provide students with whiteboards/dry-erase markers.

Notice and Wonder

- Display the first puzzle in Level 3. Ask: "What do you notice that is similar/different from the puzzle we did yesterday?"
- Allow a few students to share out.

Predict and Justify

• Ask students to think of their strategy for solving the puzzle and predict what will happen when they try it. Have students share out their predictions.

Test and Observe

• Select a student's solution to try, and watch the feedback. Ask students: "What happened when we tried that prediction? What did you see?"

Analyze and Learn

- Ask students to think about how what they saw happen compares to their prediction. Was our answer correct? What did they learn from the feedback?
- Show another puzzle, and have students discuss with a partner what they think they need to do to solve the problem.
- Try one of the students' strategies. Discuss the feedback.
- Continue to try Level 3 puzzles, and launch into a discussion with students around mixed numbers, unit fractions, and equivalence:
 - · How can you check to make sure both monsters get enough pie?
 - · How many thirds/halves/fourths are there altogether?
 - How could you write the fraction and the mixed number for monster 1 and monster 2?
 - How do you know this fraction is equivalent to this mixed number (e.g., why is 2 the same as 4/2)?

Connect and Extend

- Choose some puzzles for students to write equations for on paper or whiteboard.
- Ask students a challenge question: "What if Pie Monster got ____ more pies? How many pieces of pie would Pie Monster have now?"
- Have students solve the new problem, and then allow a few students to share their strategies and their answers.

How does the student:

- write equations and inequalities to compare fractions?
- figure out how many unit fractions are needed for the whole and for each monster?
- count unit fractions to find the total?
- understand that the a/b (b>0) fraction is equivalent to the mixed number?

Problem Solving (20-25 minutes)

Engage students in problem solving discussions. Read and discuss the problem, share student work, compare strategies, and make connections.

Problem of the Day

Joe the baker baked 7 apple pies to sell in his shop. Four people came in at the same time to buy pie. Joe sold the 7 pies to the four people. Each person got an equal amount of pie. How much pie did each person buy?

Instructional Stations (40 minutes)

Students will visit two stations today (20 minutes in each station). They will visit the other two tomorrow.

 Station 1: Small Group Instruction Work with students on the ST Math game, <i>Balance Pies</i>. Use the Problem Solving Process to discuss the game with the group. Work through Levels 2 on. Have students name fractions of pies. Discuss unit fractions and a/b (b>0) fractions. Students explore and discover how a/b (b>0) fractions are made up of a fractions of size 1/b. 	 Station 2: ST Math Puzzles Have students sign in and play ST Math puzzles. Remind students to use manipulatives and/or paper and pencil to help them solve problems. With 5 minutes left, have students stop playing and complete their Puzzle Reflection and Accomplishments Log.
 Station 3: Table Games Select Equivalent Fraction Concentration or Multiplication Connect Four. Have students play that game. Ask students to complete an Exit Ticket during the final 5 minutes. 	 Station 4: Design Challenge Have students select one of the games they played in the last module and replay it. After playing the game, have students discuss how they would change the game. Students make the changes and then try playing the game with their changes. Have them discuss how the changes affected gameplay. Did they like them? Did they not like them? Did it make it easier or harder?





My Thinking Path (5-10 minutes)

• Have students reflect on what they have learned about solving problems involving partitioning a whole into equal sections (fractions).

Puzzle Talk: Match Fractions (20-25 minutes)

process provide students with whiteboards/dry-erase markers.

Notice and Wonder

• Display the first puzzle in Level 1. Ask: "What do you notice? What do you wonder?" Allow a few students to share out.

Predict and Justify

- Ask students to predict where the rocket will go and explain their prediction.
- You may probe students by asking: "What does the numerator represent? What does the denominator represent?"

Test and Observe

• Select a student to share how to move the slider, how many parts they are dividing and coloring in, and why.

Analyze and Learn

- Ask students to explain what they learned from the feedback about numerators, denominators and partitions. Replay the puzzle, and select the same answer. This time pause the feedback. Discuss.
- Ask students to share what they learned from the feedback. How can they use what they learned in the next puzzle?
- Show the next puzzle. Move the slider across the square at the bottom, and ask students to watch the animation. Ask: "How many pieces do you want to partition this square into so that it matches the fraction in the puzzle?"
- Remind students that the denominator tells how many equal pieces the whole has been divided into: "The denominator is ____, so we need to divide the square into ____ equal parts." Select the correct denominator. Remind students that the numerator counts how many of the equal pieces you have. The numerator in the puzzle is 1, which means that we just need one of the pieces. Ask students: "How could we represent just one of the pieces?" Move the cursor over the square again to show how to shade in the pieces, and watch the feedback.
- Solve the puzzle, and watch the feedback.

How does the student:

- discuss the size and number of partitions created as the cursor moves from left to right?
- discuss the meaning of the denominator in the fractions?
- discuss the meaning of the numerator in the fractions?
- discuss unit fractions and count by unit fractions?

Problem Solving (20-25 minutes)

Engage students in problem solving discussions. Read and discuss the problem, share student work, compare strategies, and make connections.

Problem of the Day

• Gordon baked a pan of lasagna for his family of 4. He cut the lasagna into eight equal pieces. Explain how much lasagna each family member might eat.

Instructional Stations (40 minutes)

Students will visit two stations today (20 minutes in each station). They will visit the other two tomorrow.

Station 1: Small Group InstructionHave students solve the problems similar to the

- Problem of the Day and puzzles. For example:
 - Twana baked a small pan of lasagna for her family of 4. Explain how she might cut the lasagna to serve her family equal sized pieces. How much lasagna will each person get?
 - Discuss what they know in the problem and what they need to know to solve the problem.
- Bring the discussion about each problem to the equation, and discuss what each of the numbers in the equation represents.
- Ask students to compare their drawings, etc., to the numbers in the equations.

Station 3: Table Games

- Select Equivalent Fraction Concentration or Multiplication Connect Four.
- Have students play that game.
- Ask students to complete an Exit Ticket during the final 5 minutes.

Station 2: ST Math Puzzles

- Have students sign in and play ST Math puzzles.
- Remind students to use manipulatives and/or paper and pencil to help them solve problems.
- With 5 minutes left, have students stop playing and complete their Puzzle Reflection and Accomplishments Log.

Station 4: Design Challenge

- Have students complete the Game Planning Sheet (page 8 in their Design Challenge Station Booklet).
- The students will tell the name of their game, a brief description of their game is, and why they chose this type of game.





My Thinking Path (5-10 minutes)

• Have students reflect on what they have learned about solving problems involving partitioning a whole into equal sections (fractions). Students should complete the My Thinking Path reflection page in their journal.

Puzzle Talk: Match Fractions (20-25 minutes)

procus on student thinking and developing problem solving skills using the Problem Solving Process.
 provide students with whiteboards/dry-erase markers.

Notice and Wonder

- Show a puzzle from Level 2. Ask students: "What do you notice that is similar/different from the puzzles we did yesterday?"
- Have students predict how to solve the puzzle and share their prediction with a neighbor. Ask students: "Did your predictions match? What strategies did you use?"

Predict and Justify

• Have students share out. Try one of the students' ideas.

Test and Observe

• Watch the feedback together, and discuss what they saw. Discuss how the animation shows the numerator and denominator of the fraction.

Analyze and Learn

- Ask students to think about how what they saw happen compares to their prediction. What did they learn from the feedback?
- Show another puzzle from Level 2. Discuss how they determine the number of partitions to select. Ask: "Where is a unit fraction? How many unit fractions is this?"
- Have students write an addition equation to show that it takes a unit fraction of size 1/b to equal the a/b (b>0) fraction (e.g., 1/6 + 1/6 = 2/6).

Connect and Extend

- Display the next puzzle and move the cursor along the square again. Ask students to turn to a partner and discuss what happens to the size of the fraction pieces as the denominator gets bigger. How many halves/ thirds/fourths/fifths/sixths does it take to make one whole? Why? (Show that the bigger the denominator gets, the smaller the fraction pieces become.) Allow students to share their thinking whole group.
- Do a share-out, and try a student's solution, watching the feedback. Remind students that the numerator counts how many of the equal pieces you have (e.g., a numerator of 4 means that you have 1, 2, 3, 4 of the fraction pieces).
- Ask: "How many of these fraction pieces does it take to make the whole? Why?"

How does the student:

- discuss the size and number of partitions created as the cursor moves from left to right?
- discuss the meaning of the denominator in the fractions?
- discuss the meaning of the numerator in the fractions?
- discuss unit fractions and count by unit fractions?

Problem Solving (20-25 minutes)

Engage students in problem solving discussions. Read and discuss the problem, share student work, compare strategies, and make connections.

Problem of the Day

• Brett and three classmates were given a bulletin board to present their Math Challenge. They decided to divide the bulletin board so that each of them had an equal amount of space. Show two different ways they could partition the board. Prove that one partition from your first bulletin board example is equivalent to one partition from the second example.

Instructional Stations (40 minutes)

Students will visit two stations today (20 minutes in each station). They will visit the other two tomorrow.

Station 1: Small Group Instruction

- Have students solve the problems similar to the Problem of the Day and puzzles. For example:
 - Twana baked a small pan of lasagna for her family of 4. Explain how she might cut the lasagna to serve her family equal sized pieces. How much lasagna will each person get?
 - Discuss what they know in the problem and what they need to know to solve the problem.
- Bring the discussion about each problem to the equation, and discuss what each of the numbers in the equation represents.
- Ask students to compare their drawings, etc., to the numbers in the equations.

Station 3: Table Games

- Select Equivalent Fraction Concentration or Multiplication Connect Four.
- Have students play that game.
- Ask students to complete an Exit Ticket during the final 5 minutes.

Station 2: ST Math Puzzles

- Have students sign in and play ST Math puzzles.
- Remind students to use manipulatives and/or paper and pencil to help them solve problems.
- With 5 minutes left, have students stop playing and complete their Puzzle Reflection and Accomplishments Log.

Station 4: Design Challenge

- Have students complete the Game Planning Sheet (page 8 in their Design Challenge Station Booklet).
- The students will tell the name of their game, a brief description of their game is, and why they chose this type of game.





Design Challenge Station (30-40 minutes)

- Discuss the importance of rules. Ask students to describe things that we have rules for and why rules are important. How do rules impact gameplay?
- Have the students open their booklet to the Game Rules Challenge (page 9 in their Design Challenge Station Booklet).
- Ask the students to explain why rules are important.
 - Remind them of the rules they used when they played Traffic Lights Tic-Tac-Toe and Dara. What are some things that rules tell us (such as who goes first, how you move on the board, what you have to do to win, etc.).
- Discuss the game Tic-Tac-Toe. Remind students that Traffic Lights Tic-Tac-Toe is a modified version of Tic-Tac-Toe. What are the rules of the game? Have the students write the rules in their booklets.
 - It is important to help students understand how to write rules that are clear and easy for the players to understand.
- Working in teams of two, have the students change one rule for Tic-Tac-Toe, write the new rule, and play the game using that rule.
 - Discuss how gameplay was affected by their new rule. Reiterate the importance of having clear rules.
- Inform the students that writing rules is only part of what they need to plan for their game.
- They are going to be working on blueprints. Review pages 10-13 in the Design Challenge Station Booklet with the students. Explain that blueprints allow them to plan out each part of their game so that it is easier to build. Let students know that they will be working on their blueprints, creating a sketch of their game, and writing their rules.
- Share with students that on page 14 of the Design Challenge Station Booklet they will begin assigning jobs to team members to build their game. As they make their blueprint, they can start to think about who will have the job of making the game board, who will make the game cards or game pieces, who will write out all the rules that the group decides on, etc. It is important that everyone in the group helps build the game.
- After reviewing the booklet with the students, give them time to begin their blueprints.

Whole Group Table Games (15-20 minutes)

During this time you will introduce Number Line Fraction Bingo and Final Countdown. Students will play these games in the next module in Station 3.

- Introduce one of the games.
- After explaining the game and playing it with the whole group, give students time to play it on their own.
- After playing the game, have them discuss:
 - What math did they learn or use?
 - What strategies did they try to win the game?
- Repeat with the second game.

Optional: ST Math Activity Page (15 minutes)

ST Math Activity Page

- Project the game, *Pie Monster*.
- Play a few puzzles to help students understand the game.
- Have students turn to the ST Math Activity Page: Pie Monster.
- Ask students what they notice about the content on the page. What do they wonder? Where do they want to start on the page?
- Give them time to complete the page.
- Discuss the page ,and have students share their thinking.
- Take the time to compare strategies, and have students share their work.
- Make connections to the game.

Focused Instructional Time (20 minutes)

Focused Instructional Time

- During this station time, students do not rotate. They can either be assigned to a station or allowed to choose one to go to.
- This is an excellent opportunity to pull students who need additional support to Station 1: Small Group Instruction, where they can work with the teacher on concepts they are struggling with. Use the <u>Teacher</u> <u>Planner</u> to help target this time with students.

 Station 1: Small Group Instruction Identify specific students for intervention or extension. Choose the ST Math puzzle or problem solving question that the students struggled with. You may choose to use the Teacher Planner to help you plan your instruction. 	 Station 2: ST Math Puzzles Have students sign in and play ST Math puzzles. Remind students to use manipulatives and/or paper and pencil to help them solve problems. With 5 minutes left, have students stop playing and complete their Puzzle Reflection and Accomplishments Log.
 Station 3: Table Games Allow students to choose one of the games they have learned. Have students play that game. Ask students to complete an Exit Ticket during the final 5 minutes. 	 Station 4: Design Challenge Allow students to continue to work on their blueprints. Once students have completed their blueprints, they need to create their rules and directions and assign the task of building the game to different members of their team. Remind students that they can record the jobs that need to be done on page 14 of the Design Challenge Station Booklet.

Closing (10 minutes)

Thinking and Reflecting Time

- Have students complete the Post-Quiz (optional).
- Engage students in discussions about what they have learned in this module, what they have questions about, and what they would like to learn more about.
- Have students review ST Math Problem Solving Journal pages for the module: My Thinking Path, Problem of the Day, Exit Tickets, and Puzzle Reflections.

